

RgeoJSD: robust noise-tolerant loss for cerebral emboli classification

Medical Imaging Research Laboratory

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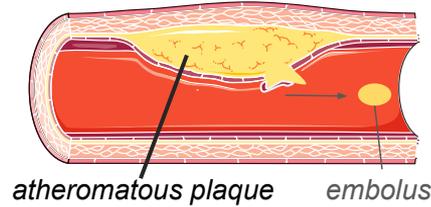
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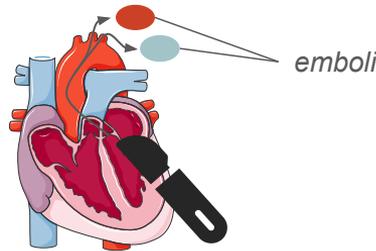
Cerebral emboli

Cerebral emboli are solid or gaseous material in the cerebral blood flow, and are one of the main risk of stroke.

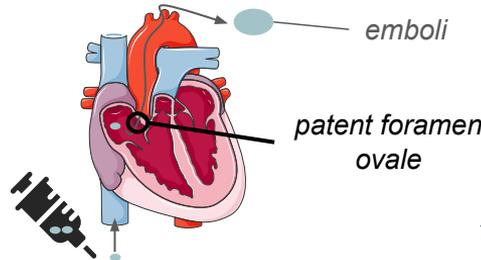
Pathology
(Atherosclerosis)



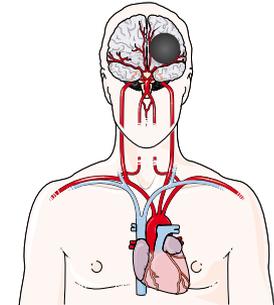
Surgical operation
(TAVI)



Micro-bubbles injection procedure
(PFO detection)



Solid or gaseous emboli
circulating in cerebral blood flow



Potential ischemic stroke

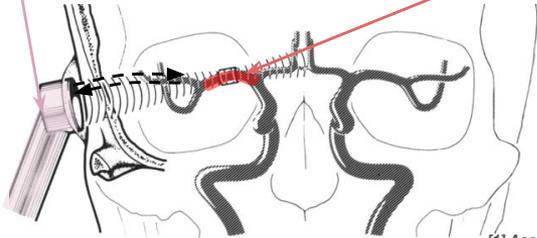
PFO = Patent Foramen Ovale (hole between left and right atriums)
TAVI = Transcatheter Aortic Valve Implantation (percutaneous endovascular technique of aortic valve replacement)



Transcranial Doppler (TCD)

ultrasound probe

right cerebral middle artery



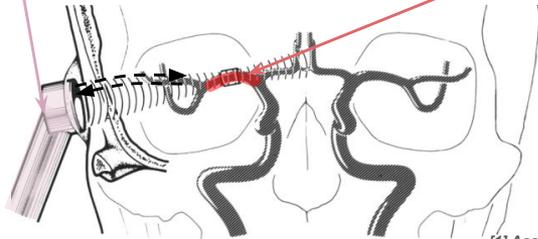
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[2] Guépié B. K. et al., IEEE JBHI, 2018 Sequential Emboli Detection from Ultrasound Outpatient Data

Transcranial Doppler (TCD)

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[1] Aaslid et al., JNS, 1982

Portable and robotized TCD



Atys
medical

Longer recordings with low constraints for the patient [2]

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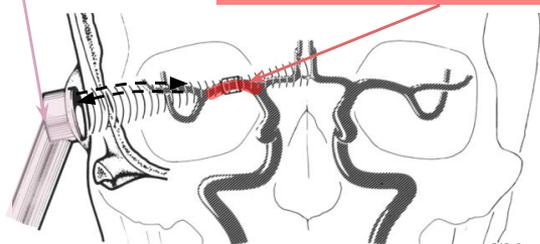
Emboli detection

Transcranial Doppler is a unique non-invasive modality to monitor emboli, detected as high intensity transient signals.

Transcranial Doppler (TCD)

ultrasound probe

right cerebral middle artery



[1] Aaslid et al., JNS, 1982

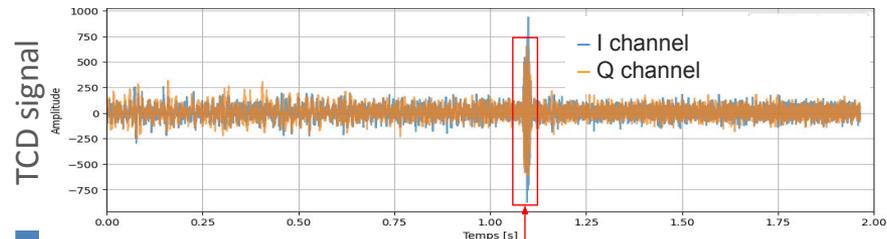
Portable and robotized TCD



Atys medical

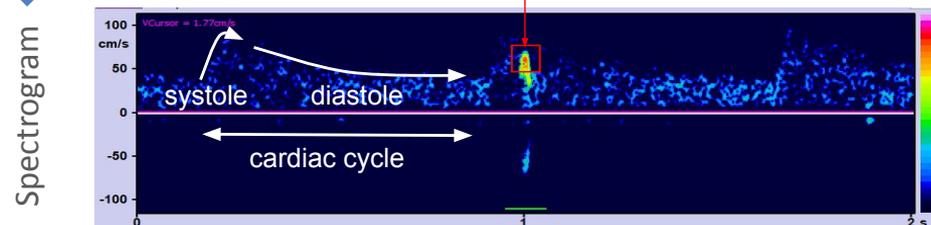
Longer recordings with low constraints for the patient [2]

High Intensity Transient Signal (HITS)



FFT

Same HITS, 2 representations

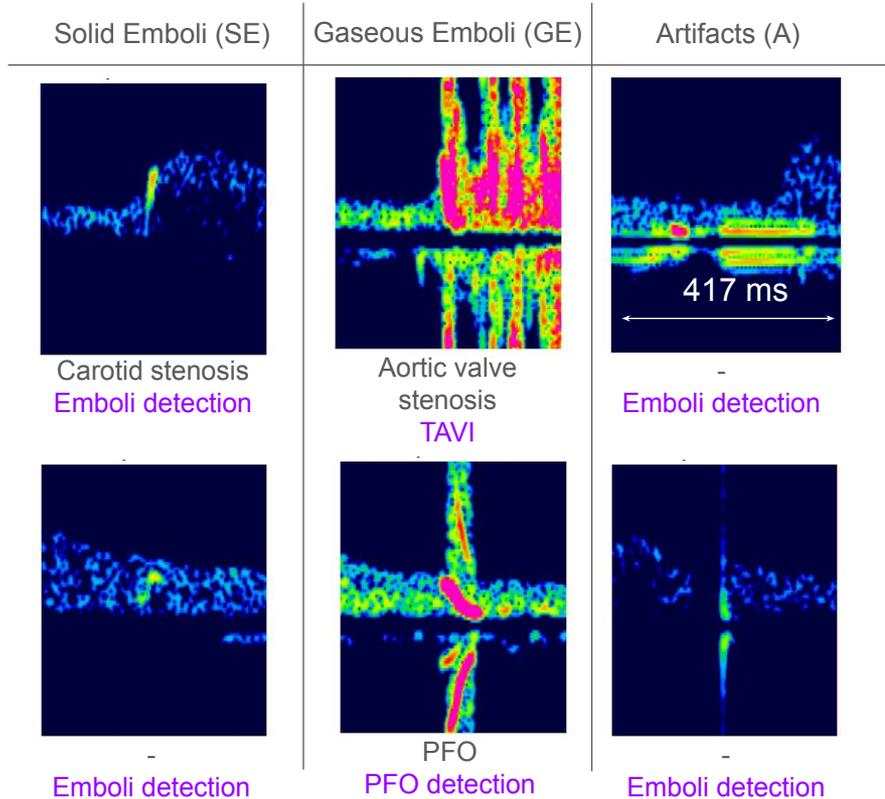


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Emboli classes

Medical interest is to distinguish between artefact / emboli (counting) and solid emboli / gaseous emboli (risk, causes).



International consensus 1998
→ duration < 300 ms
→ intensity increase > 3 dB
w.r.t blood flow signal
→ unidirectional
→ musical “chirp”, “snap” sound

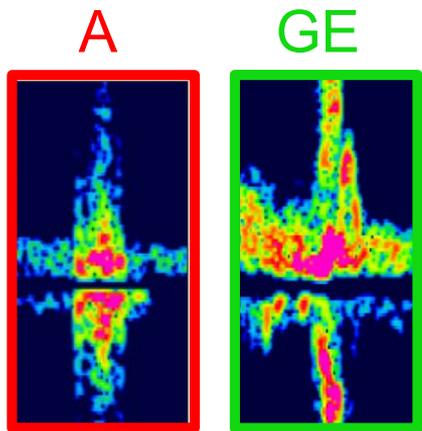
Ringelstein E. B. et al., Stroke, 1998
Consensus on microemboli detection by TCD

Our main objective: deep learning for HITS classification A/SE/GE

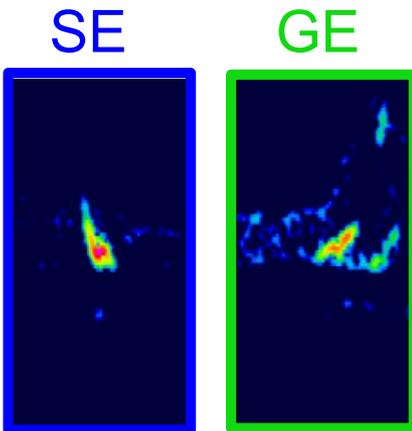


Ambiguous cases

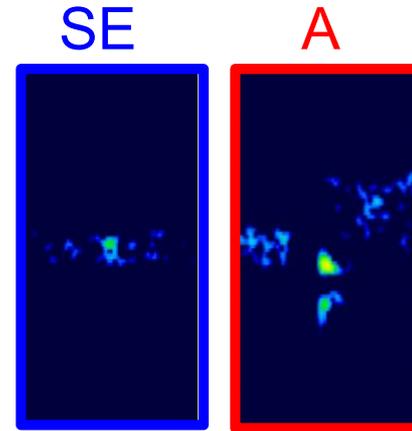
Annotation can be difficult because of ambiguous signal and annotator subjectivity.



scalpel noise vs. emboli shower



Speed modulation ambiguity

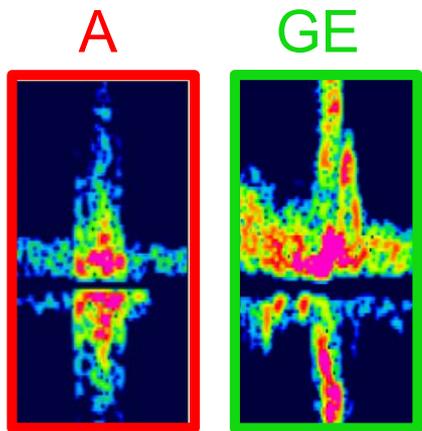


Small solid emboli vs. speckle and other artifacts

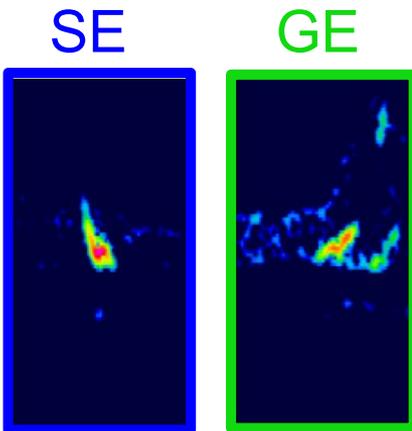


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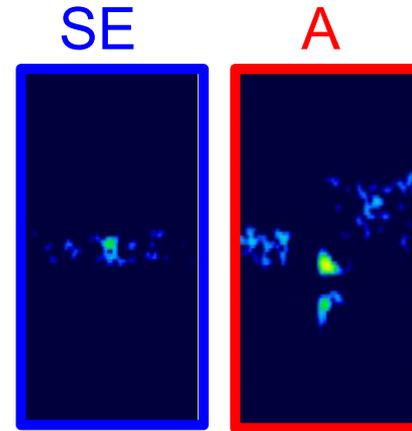
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Speed modulation ambiguity



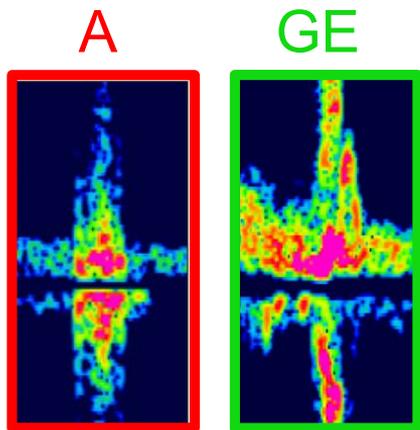
Small solid emboli vs. speckle and other artifacts

Challenge for supervised learning
Designing methods that are robust to label noise

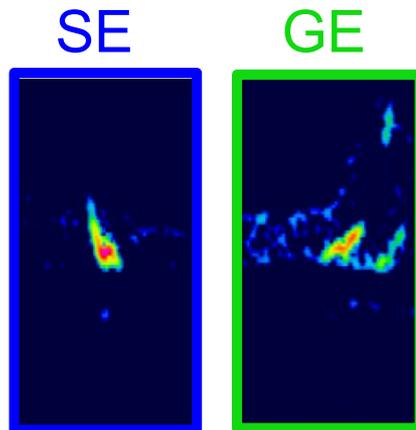


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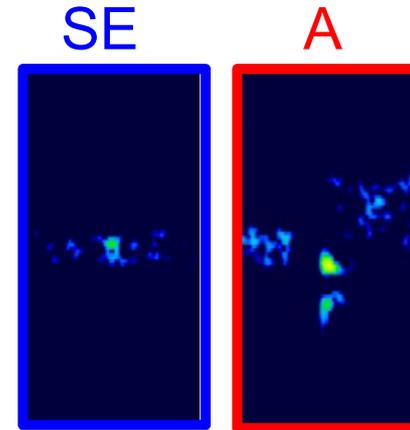
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Speed modulation ambiguity



Small solid emboli vs. speckle and other artifacts

Challenge for supervised learning

Designing methods that are robust to label noise

Our proposition

RgeoJSD, new label robust loss function for classification

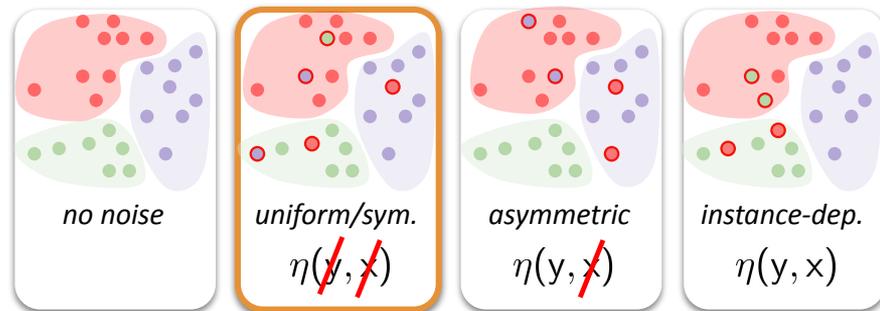


Robust losses

Loss functions robust to noisy labels are a way to deal with noisy labels that is architecture-free and computationally light.

Noise rate η

$$\eta(y, x) = \text{p}(\overset{\text{noisy label}}{y_\eta} \neq \overset{\text{true label}}{i} | \underset{\text{sample}}{y = i, x})$$

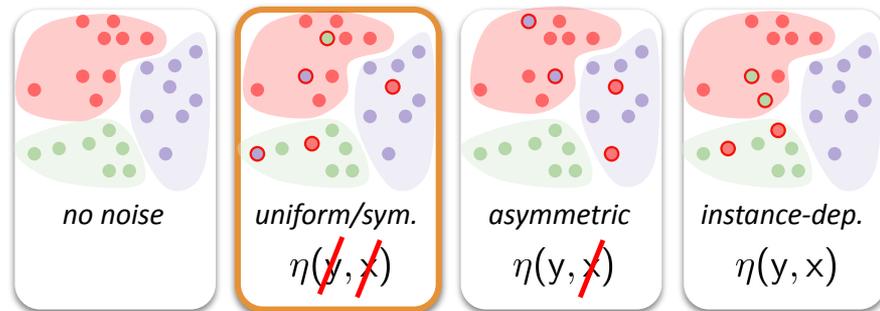


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Noise tolerant loss

$$\mathbb{P}_{\text{clean}}[f^*(\mathbf{x}) = y_{\mathbf{x}}] = \mathbb{P}_{\text{clean}}[f_{\eta}^*(\mathbf{x}) = y_{\mathbf{x}}]$$

Minimizer of clean risk Minimizer of noisy risk



Robust losses

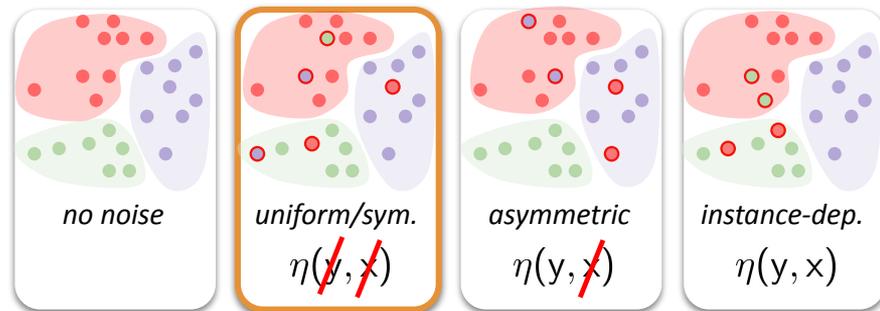
Loss functions robust to noisy labels are a way to deal with noisy labels that is architecture-free and computationally light.

Noise rate η

$$\eta(y, x) = \mathbb{P}(y_\eta \neq i | y = i, x)$$

noisy label true label

sample



Noise tolerant loss

$$\mathbb{P}_{\text{clean}}[f^*(\mathbf{x}) = y_{\mathbf{x}}] = \mathbb{P}_{\text{clean}}[f_\eta^*(\mathbf{x}) = y_{\mathbf{x}}]$$

Minimizer of clean risk Minimizer of noisy risk

Sufficient conditions [3]

Symmetric loss L [3]

“Reasonable” noise rate $\eta < \underbrace{\frac{K}{K-1}}_{0.66 \text{ for } K=3 \text{ classes}} \Rightarrow L \text{ is noise tolerant under uniform label noise}$



Geometric Jensen-Shannon Divergence (GeoJSD) [4]

$$\text{GeoJSD}(f(x), y) = (1 - \alpha)\text{KL}(f(x)||m) + \alpha\text{KL}(e_y||m)$$

$$m = f(x)^{1-\alpha} e_y^\alpha$$



Geometric Jensen-Shannon Divergence (GeoJSD) [4]

$$\begin{aligned}\text{GeoJSD}(f(x), y) &= (1 - \alpha)\text{KL}(f(x)||m) + \alpha\text{KL}(e_y||m) & m &= f(x)^{1-\alpha}e_y^\alpha \\ &= \alpha(1 - \alpha)[H(e_y, f(x)) - H(f(x), f(x)) + H(f(x), e_y) - H(e_y, e_y)]\end{aligned}$$



Geometric Jensen-Shannon Divergence (GeoJSD) [4]

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$$m = f(x)^{1-\alpha} e_y^\alpha$$

$$= \alpha(1 - \alpha) \left[\underbrace{H(e_y, f(x)) - H(f(x), f(x))}_{\propto \text{cross-entropy}} \right] + \underbrace{H(f(x), e_y) - H(e_y, e_y)}_{\propto \text{reverse cross-entropy}}$$

\Rightarrow convergence properties

\Rightarrow symmetric loss
 \Rightarrow label noise tolerant



Geometric Jensen-Shannon Divergence (GeoJSD) [4]

$$\begin{aligned} \text{GeoJSD}(f(x), y) &= (1 - \alpha)\text{KL}(f(x)||m) + \alpha\text{KL}(e_y||m) & m &= f(x)^{1-\alpha} e_y^\alpha \\ &= \alpha(1 - \alpha) \underbrace{[H(e_y, f(x)) - H(f(x), f(x))]}_{\propto \text{cross-entropy}} + \underbrace{[H(f(x), e_y) - H(e_y, e_y)]}_{\propto \text{reverse cross-entropy}} \\ &\Rightarrow \text{convergence properties} & \Rightarrow \text{label noise robustness} \end{aligned}$$

\propto cross-entropy
 \propto reverse cross-entropy
 \Rightarrow convergence properties
 \Rightarrow symmetric loss

 \Rightarrow label noise robustness

Robust GeoJSD (RgeoJSD)

$$\text{RgeoJSD}(f(x), y) = \underbrace{\beta}_{\text{NEW}} \cdot L_C + \underbrace{\gamma}_{\text{NEW}} \cdot L_R$$



Dataset

We used a private dataset of spectrograms from TCD recordings in different hospitals.

Dataset

Spectrograms (400 ms)

1232 RGB images (160×192×3)

 35 subjects (21-85 y.o.)

 10 hospital sources  5 FR, 5 EU

 various services

 various examinations

 various causes

Acquisition



TCD-X Robotized Holter

1.5MHz, PRF ~6kHz

Volume 8-22 mm³

Depth 45-55mm

HBR detection [2]

Train set (839 HITS, 68%)

Gaseous Emboli

30,4%

255

256

Artifacts

30,5%

Solid Emboli

39,1%

328

Test set (393 HITS, 32%)

Gaseous Emboli

33,6%

132

142

Artifacts

36,1%

Solid Emboli

30,3%

119

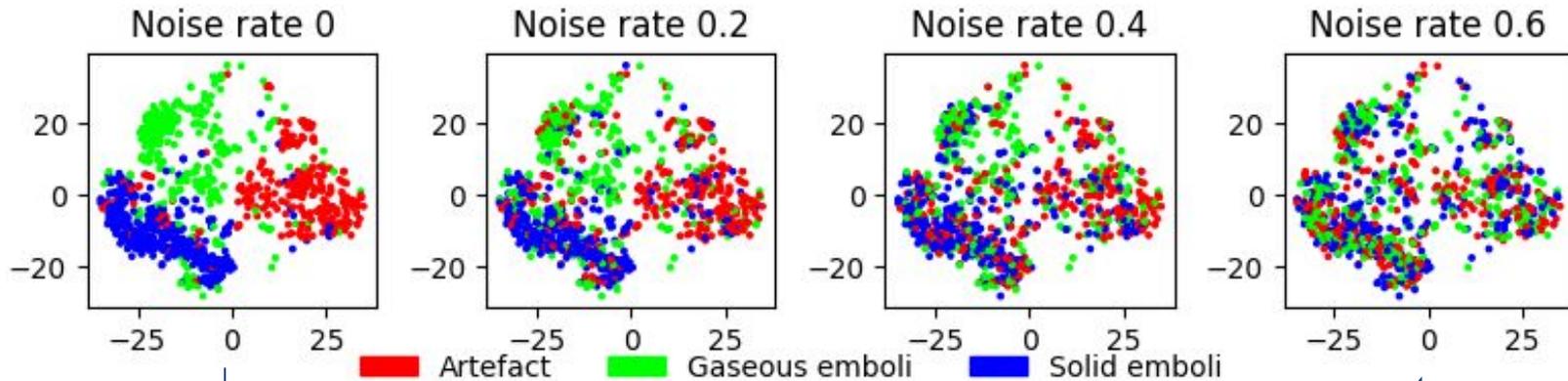
[2] Guépié B. K. et al., IEEE JBHI, 2018 Sequential Emboli Detection from Ultrasound Outpatient Data



Adding noise

Uniform label noise is synthetically added with a noise rate η .

$$p(\overset{\text{noisy}}{y_\eta = i} | \overset{\text{true}}{y = j}) = \begin{cases} 1 - \eta & \text{if } i = j \\ \eta/2 & \text{if } i \neq j \end{cases} \quad \text{noise rate}$$



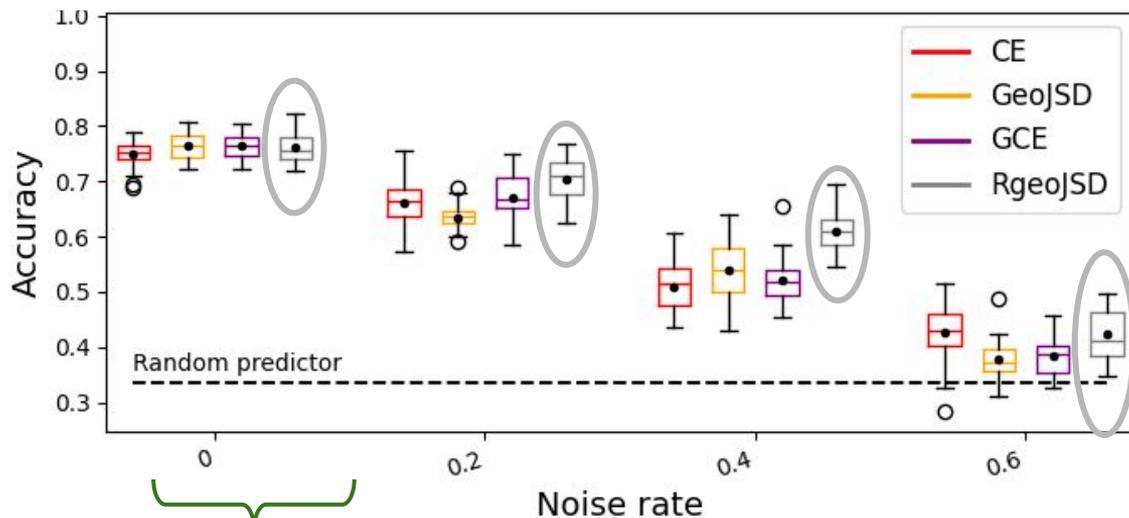
Point cloud using t-SNE on classifier latent space

Coloring points for different noise rates



Classification performance

Accuracy on test set (20 runs)



Similar performances under no noise

Best method for medium noise rates

Performance drop for high noise rate

$$CE(f(x), y) = H(f(x), y)$$

$$GeoJSD(f(x), y) = \alpha' L_C + \alpha' L_R$$

$$\alpha' = 0.25$$

$$GCE(f(x), y) = \frac{1 - f_y(x)^q}{q} \quad q = 0.7$$

$$RgeoJSD(f(x), y) = \beta \cdot L_C + \gamma \cdot L_R$$

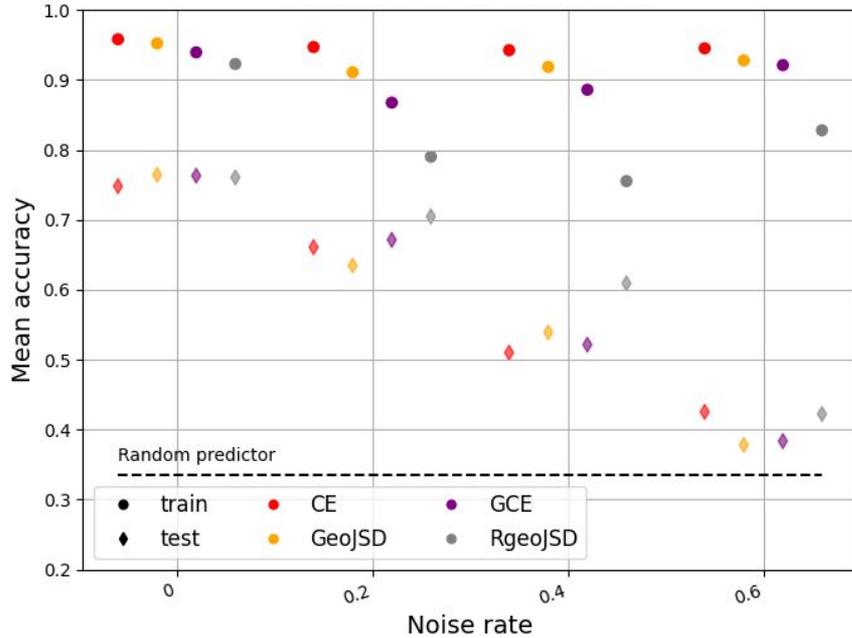
$$\beta = 2.5 \cdot 10^{-4} \quad \gamma = 2.5 \cdot 10^{-2}$$

+ global performance drop
+ global dispersion



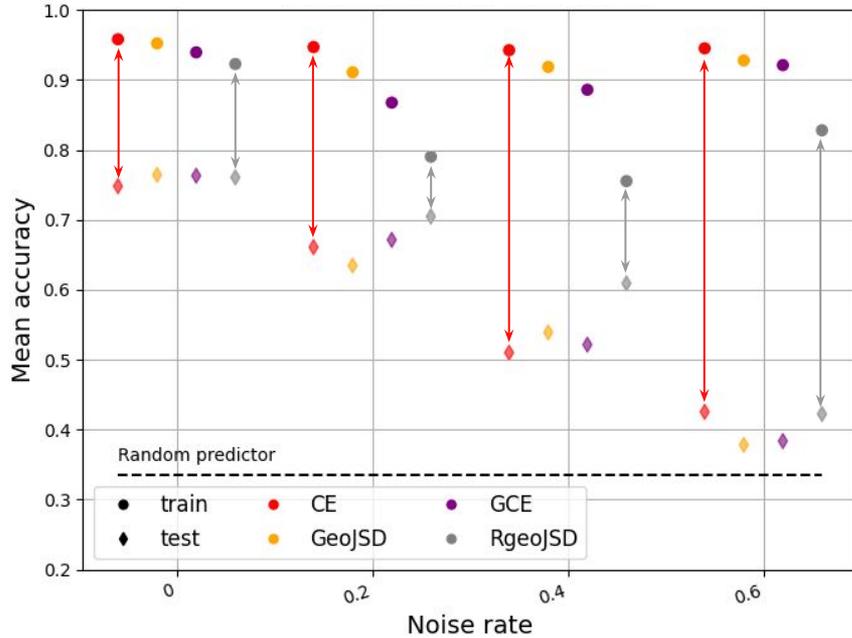
Training behavior

Mean accuracy on test set (20 runs)



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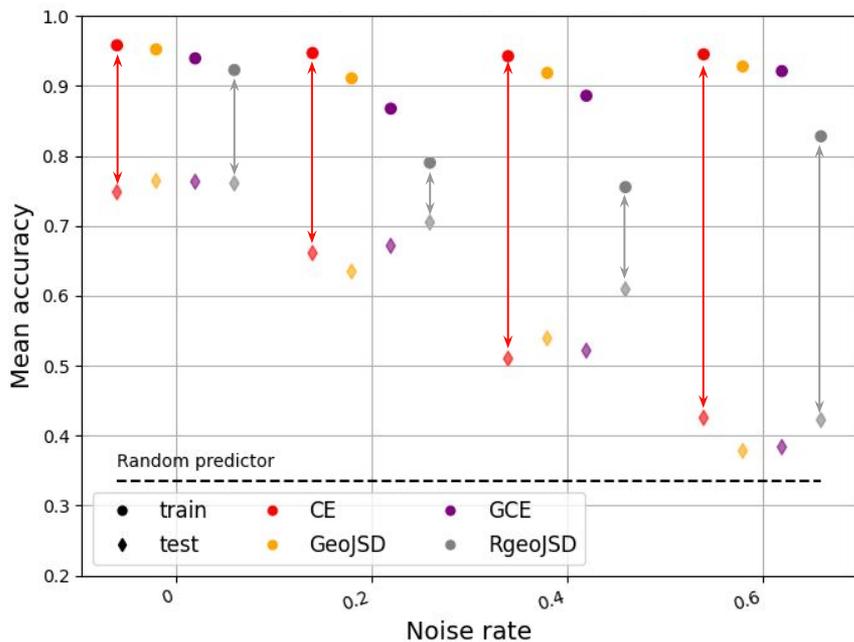


⇒ Symptomatic of overfitting



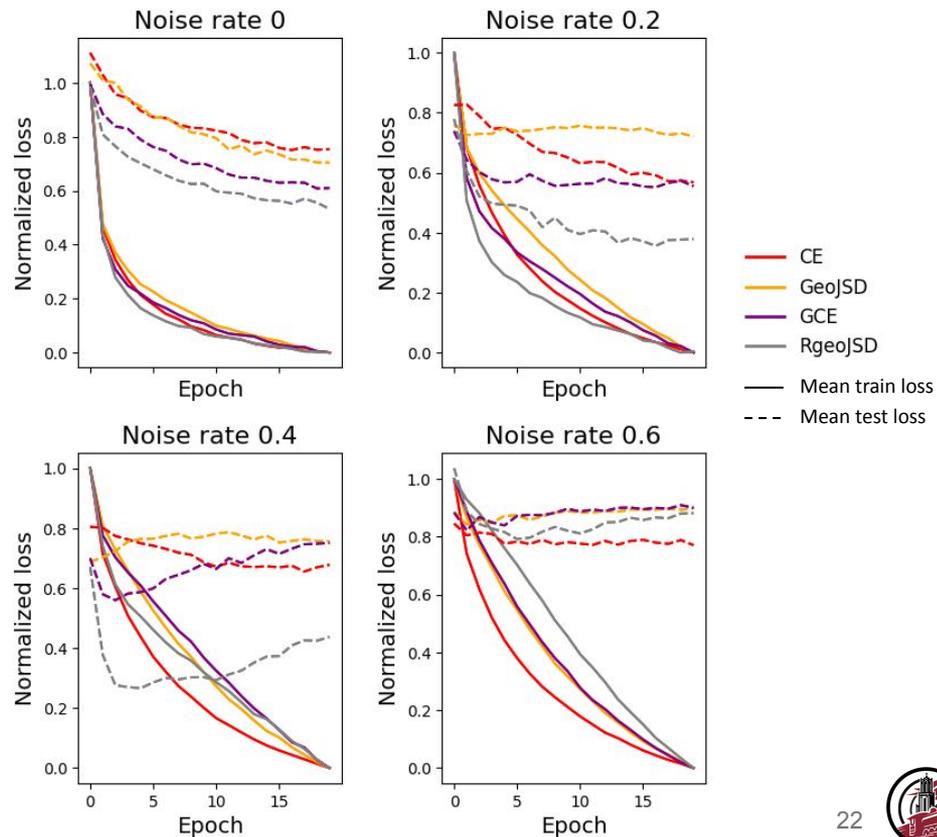
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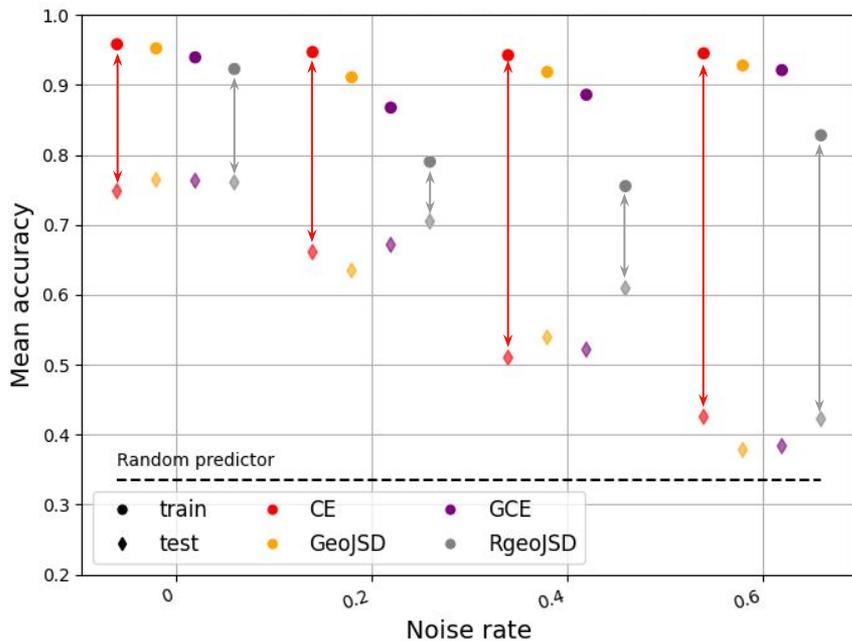
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Mean train and test losses over 20 runs



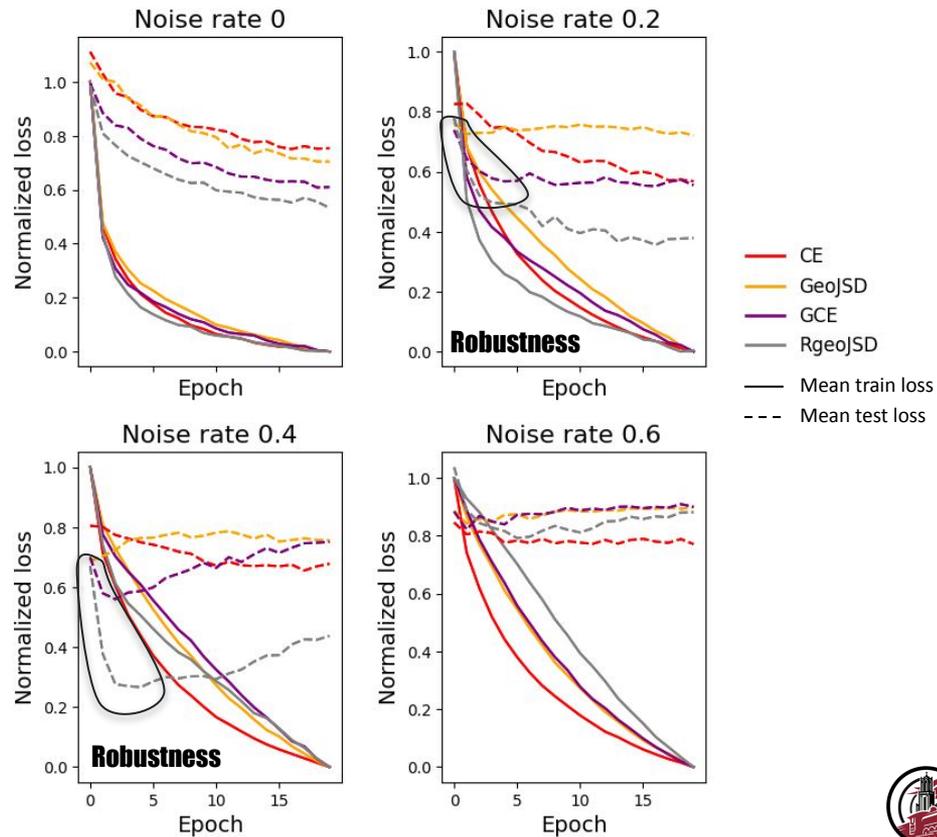
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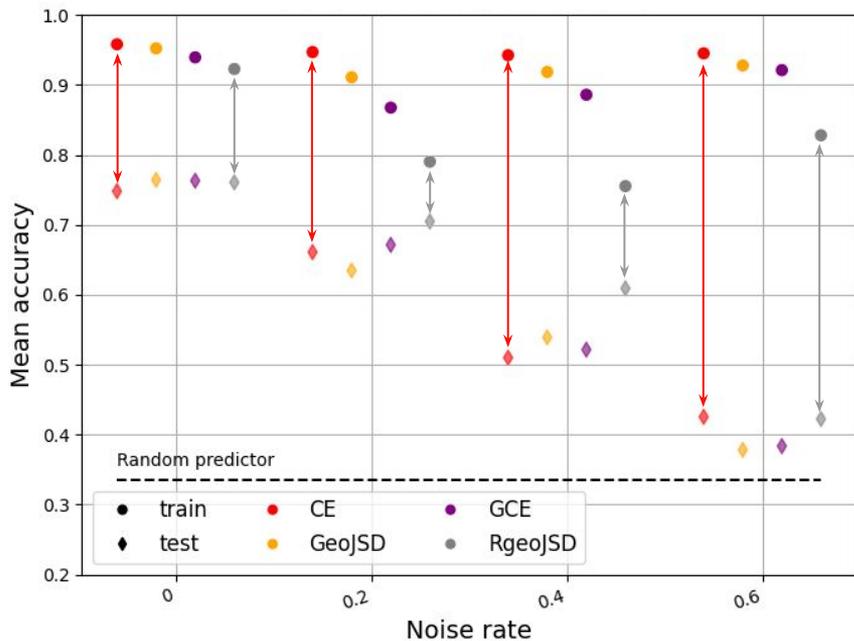
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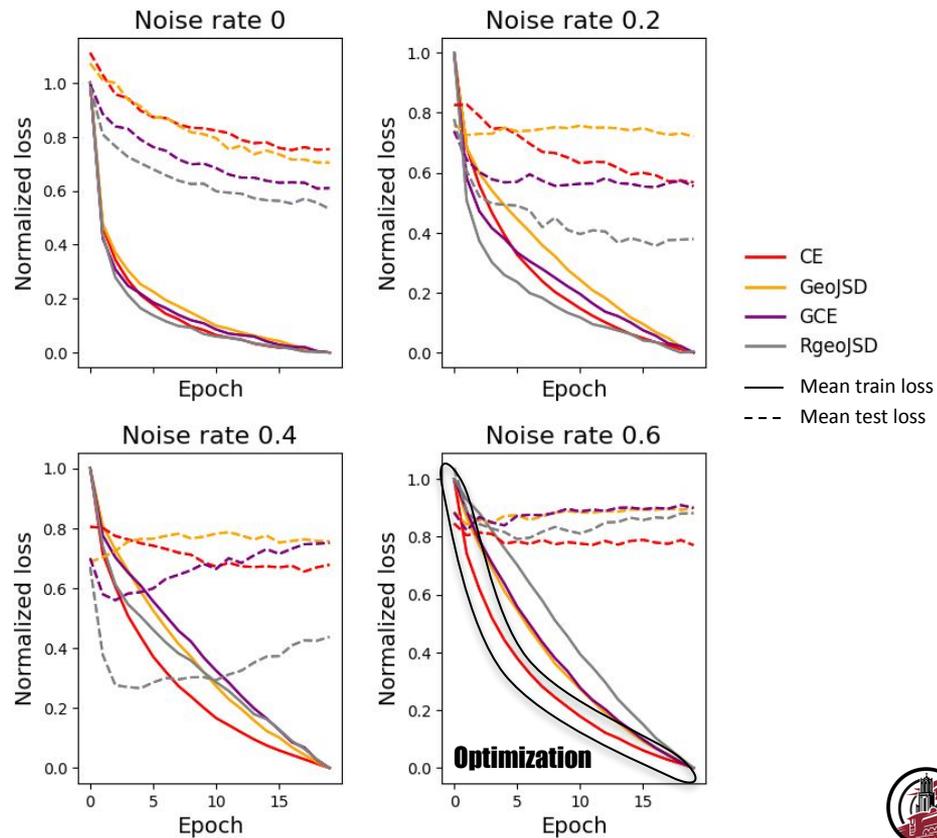
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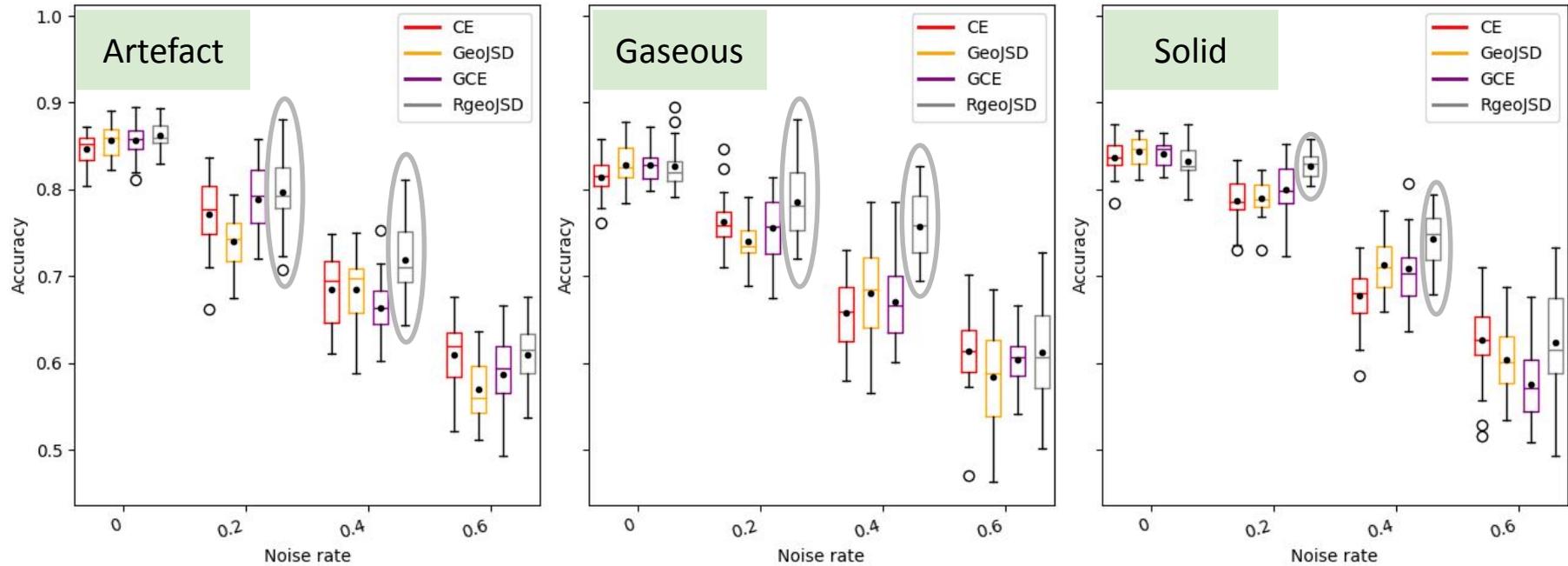
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Mean train and test losses over 20 runs



Classification performance

Accuracy on test set (20 runs)



- At medium noise rates, our method is better on all classes
- Higher dispersion of accuracy for SE and GE at high noise rates



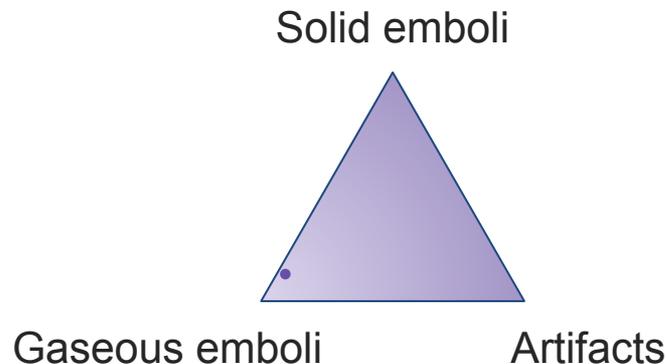
Conclusion

- New loss tolerant to label noise
- Easy and efficient implementation
- Best performances on our TCD dataset for medium noise rates (uniform noise)
- Same performance under no noise

$$R_{\text{geoJSD}}(f(x), y) = \beta \cdot L_C + \gamma \cdot L_R$$

Perspectives

- Illustrate weights effect
- Test on other types of noise
- Study the impact on model uncertainty



Thanks for your attention, any question ?

Take home messages

- TCD data needs a particular care regarding label noise
- Classification loss similar to cross-entropy while more robust to label noise

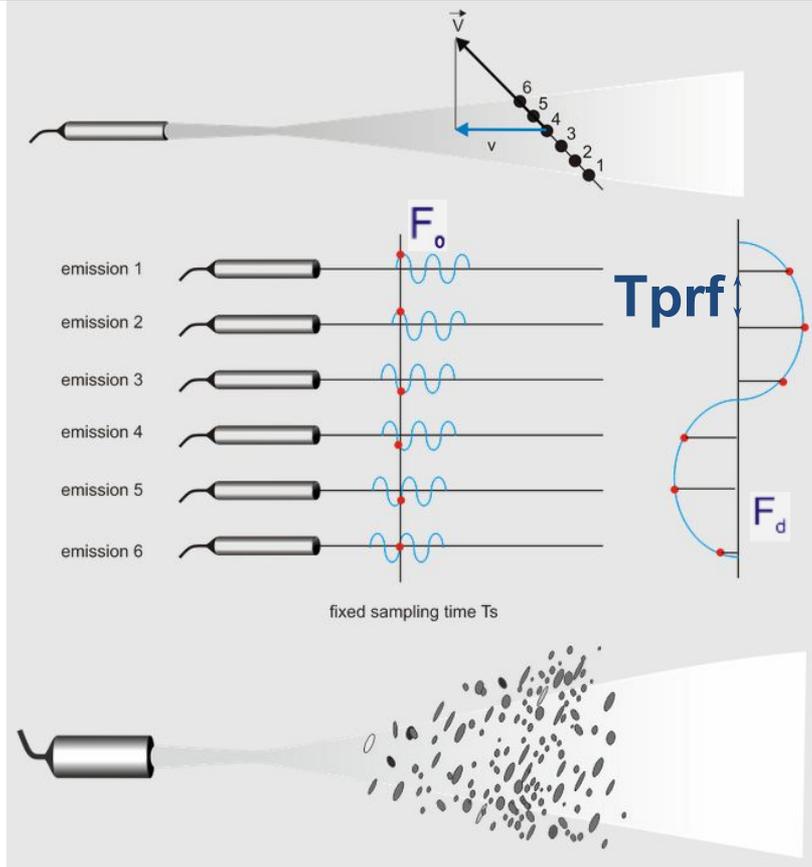
Proceeding available



<https://hal.science/hal-05234901>

Contact: mathilde.dupouy@insa-lyon.fr

TCD acquisition



Speed wrt measured frequency

$$V = \frac{F_d * C}{2 * F_o * \text{Cos } \delta}$$

Max. speed wrt PRF

$$V_{\text{max}} = \frac{F_{\text{prf}} * C}{4 * F_o * \text{Cos } \delta}$$

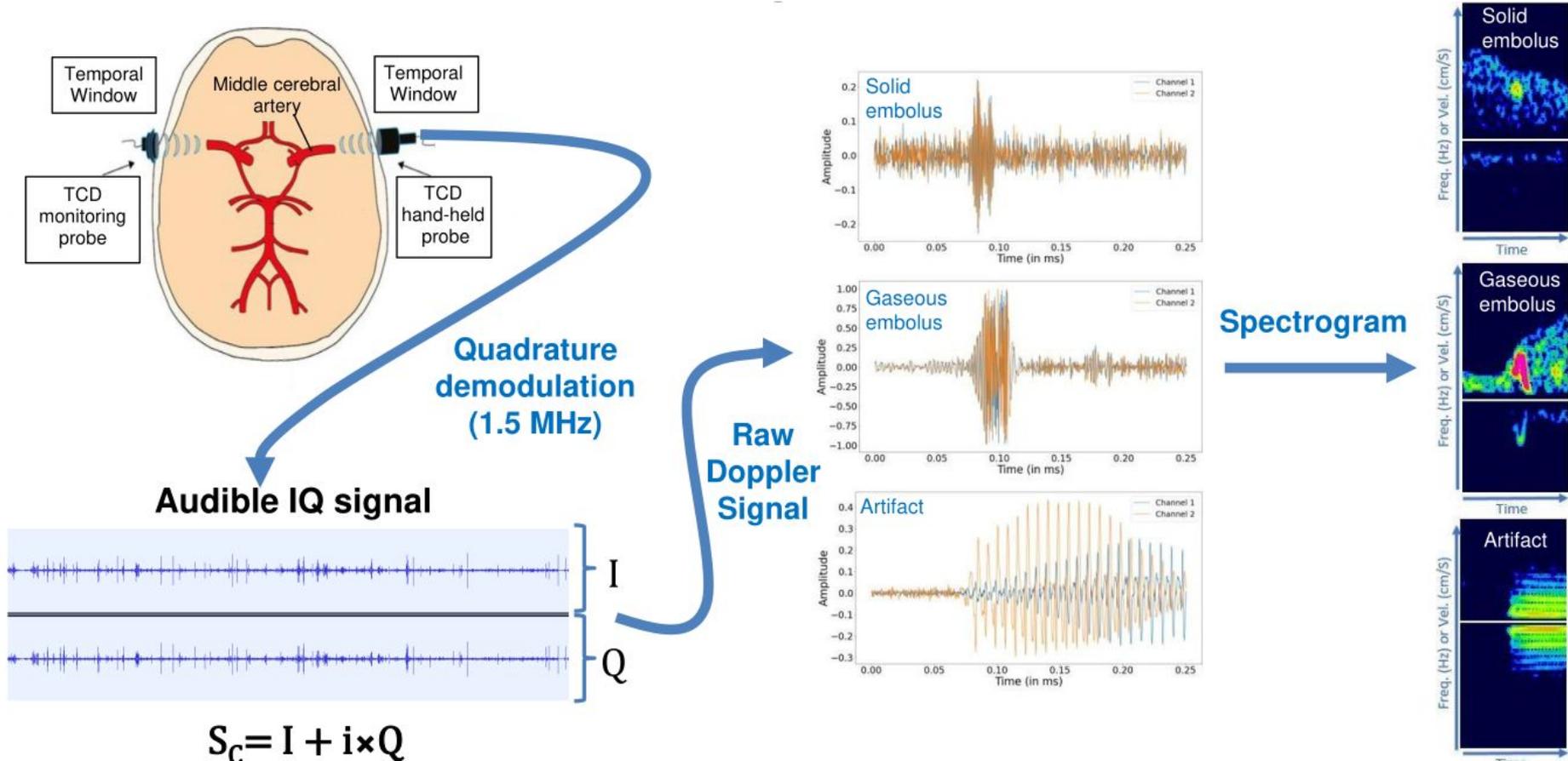
Depth wrt PRF

$$P_{\text{max}} = \frac{C}{2 * F_{\text{prf}}}$$

Doppler effect for pulsed echography

- Pulse repetition frequency: 4.4-6.2 kHz;
- Transmitted ultrasound frequency: 1.5 MHz;
- Insonation depth: 45 – 55 mm;
- Sample volume: 8 – 10 mm³.

TCD acquisition



$$D_{\text{KL}}(P \parallel Q) = \sum_{x \in \mathcal{X}} P(x) \log \frac{P(x)}{Q(x)}.$$

How well Q approximates the true distribution P, the information gain achieved if P would be used instead of Q which is currently used.

$$H(p, q) = - \sum_{x \in \mathcal{X}} p(x) \log q(x).$$

Measures how well the distribution at hand q approximates the true distribution p.

$$H(p, q) = H(p) + D_{\text{KL}}(p \parallel q)$$

$$(\text{Geo})\text{JSD}(f(x), y) = (1 - \alpha)\text{KL}(f(x) \parallel \mathbb{m}) + \alpha\text{KL}(e_y \parallel \mathbb{m})$$

Jensen-Shannon divergence is derived from KL and is symmetric (arguments invertible) with finite values. Its square root is a metric. Its value is lower when distributions are closer.

The geometric Jensen-Shannon divergence is a variation that yields a closed-form formula for divergence between two Gaussian distributions.

Risk and symmetric loss

Noise tolerant loss

$$\mathbb{P}_{\text{clean}}[f^*(\mathbf{x}) = y_{\mathbf{x}}] = \mathbb{P}_{\text{clean}}[f_{\eta}^*(\mathbf{x}) = y_{\mathbf{x}}]$$

Minimizer of clean risk

Minimizer of noisy risk

Risk

$$R_L(f) = \mathbb{E}_{\mathbf{x}, y} [L(f(\mathbf{x}), y_{\mathbf{x}})]$$

Symmetric loss [3]

$$\text{Symmetric loss } L \quad \exists C, \forall f, \forall \mathbf{x}, \sum_{k=1}^K L(f(\mathbf{x}), k) = C$$

number of classes

+ reasonable noise rate

$$\eta < \frac{K}{K-1}$$

⇒ Robustness to uniform label noise

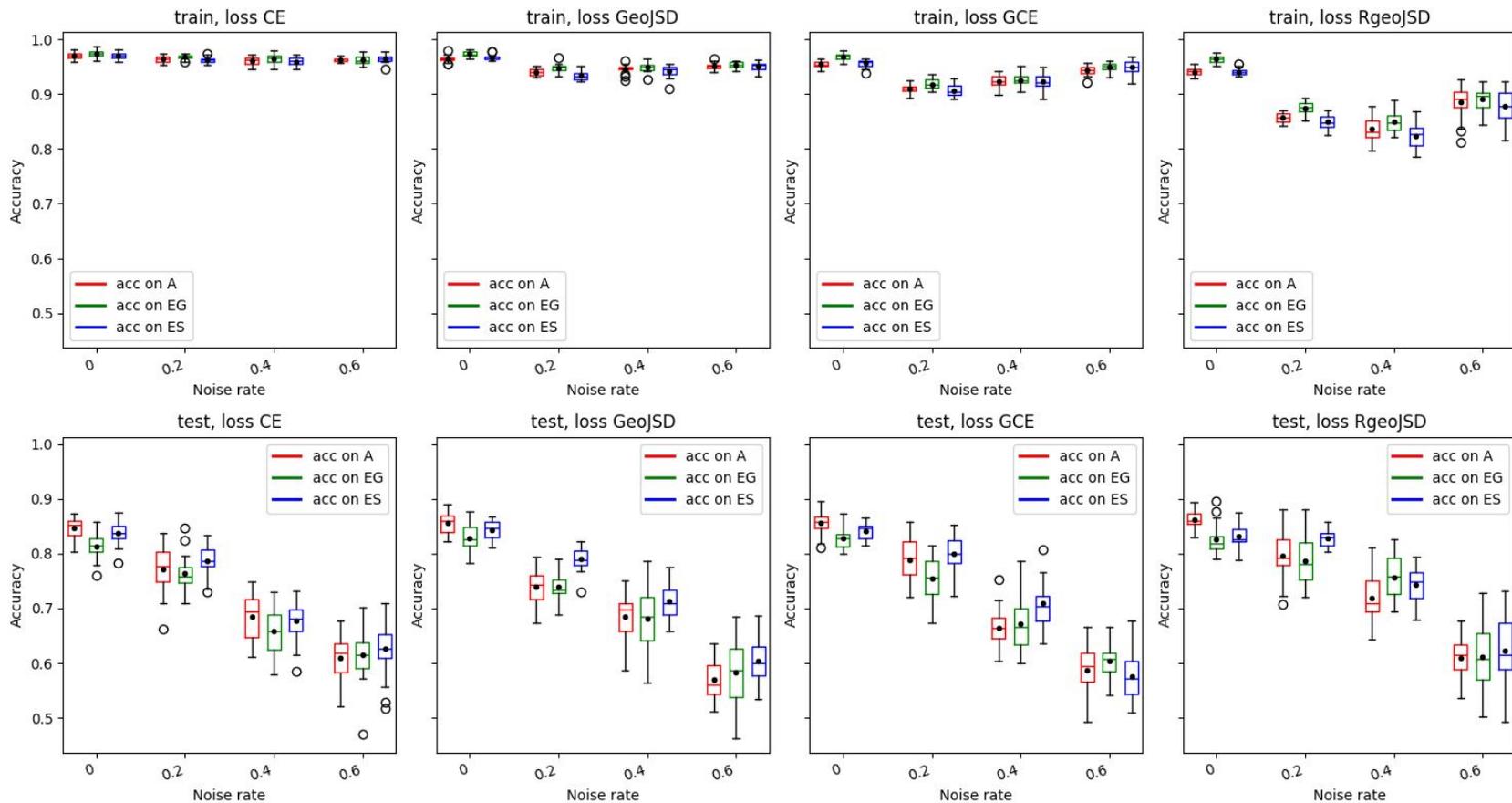
⇒ Bounded risk under simple non-uniform noise

+ true minimizer cancels out the risk

⇒ Robustness to simple non-uniform noise

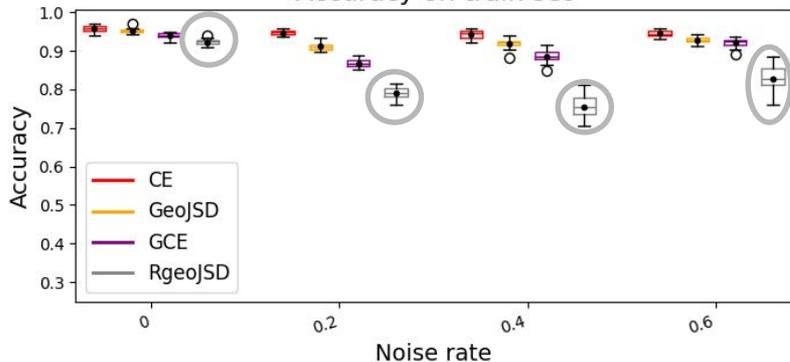


Classification performance

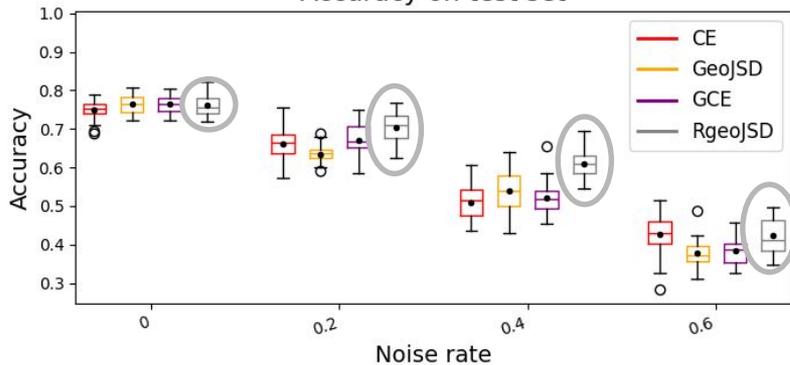


Training behavior

Accuracy on train set



Accuracy on test set



⇒ Symptomatic of overfitting

Mean train and test losses over 20 runs

